

**Precalculus A**

**4.3 Trigonometry Extended: The Circular Functions**

**Day 1**

**Hw: 4.3 Assignment #5**

D. Paulson

**Objectives:**

- SWBAT determine coterminal angle measures for any angle given in both degrees and radians.
- SWBAT determine the quadrant location of any angle.
- SWBAT determine the reference angle for any angle given in both degrees and radians.
- SWBAT evaluate all six trigonometric functions given a point on a circle.
- SWBAT determine the exact value of all points on the 16-point unit circle.

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**Coterminal Angles**

Coterminal angles are angles that share a terminal side. Since they share a terminal side you can  $\pm 360^\circ$  or  $\pm 2\pi$  as much as you want.

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**Examples**

Find a positive and a negative coterminal angle for the following. Leave answers in the original format.

$200^\circ =$

$200 + 360 =$

$200 + 360 + 360 =$

$200 - 360 =$

$200 - 360 - 360 =$

$-240^\circ =$

$120^\circ; 480^\circ$

$600^\circ; -960^\circ$

$560^\circ; -160^\circ$

$920^\circ; -520^\circ$

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### Examples

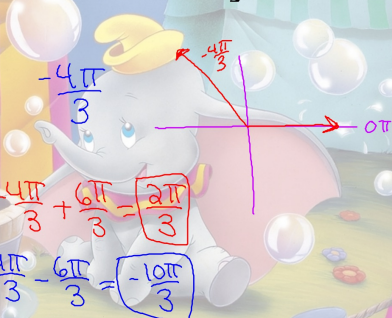
Find a positive and a negative coterminal angle for the following. Leave answers in the original format.

$$\frac{-4\pi}{3} =$$

$$\frac{-4\pi}{3}$$

$$\frac{-4\pi}{3} + \frac{2\pi}{1} = \frac{-4\pi}{3} + \frac{6\pi}{3} = \frac{2\pi}{3}$$

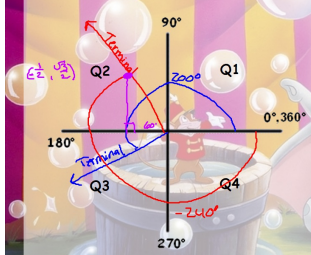
$$\frac{-4\pi}{3} - \frac{2\pi}{1} = \frac{-4\pi}{3} - \frac{6\pi}{3} = \frac{-10\pi}{3}$$



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### Location of an Angle

The location of an angle is very important in determining if the function will be positive or negative. A plane can be divided into four quadrants as shown below.



Determine the location of the following angles.

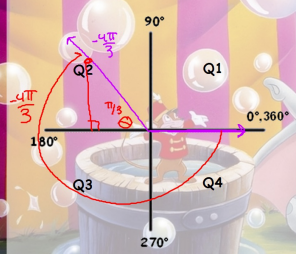
$$200^\circ = Q3$$

$$-240^\circ = Q2$$

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### Location of an Angle

The location of an angle is very important in determining if the function will be positive or negative. A plane can be divided into four quadrants as shown below.



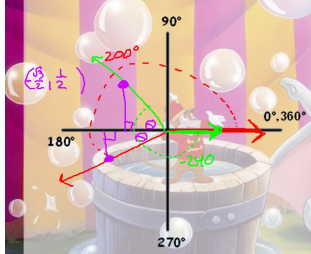
Determine the location of the following angles.

$$-\frac{4\pi}{3} = Q2$$

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### Reference Angles

Reference angles are angles formed between the terminal ray of an angle and the closest x-axis. Always the x-axis never the y-axis.



Determine the reference angle for the following:

$$200^\circ = 20^\circ$$

$$-240^\circ = 60^\circ$$

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## Reference Angles

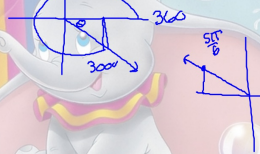
Determine the reference angle for the following:

$$135^\circ = 45^\circ$$

$$300^\circ = 60^\circ$$

$$\frac{5\pi}{6} = \frac{\pi}{6}$$

$$\frac{4\pi}{3} = \frac{2\pi}{3}$$



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